Prof. Dr. Alfred Toth

Triads and trichotomies as adjunctions

According to Toth (2009), instead of introducing prime-signs in the following static manner (cf. Bense 1980)

PS = {.1., .2., .3.),

I have suggested the following dynamic introduction of prime-signs:

PS = <[[[0, 1], [[0, 2], [0, 3]]]]>

with

$$\underbrace{\overset{\bullet}{0}\;\text{———}\;\overset{\bullet}{1}}_{\alpha_{0,1}}\underbrace{\;\text{———}\;\overset{\bullet}{2}}_{\alpha_{1,2}}\underbrace{\;\text{———}\;\overset{\bullet}{3}}_{\alpha_{2,3}}$$

If we write, as usual, the prime-signs as row and a column, we get the following categorial semiotic 3 × 3 matrix which differs considerably from the hitherto used categorial matrices in semiotics (cf. Toth 1997, pp. 21 ss.; 2008, pp. 159 ss.):

	$\alpha_{0,1}$	$\alpha_{1,2}$	$\alpha_{2,3}$
$\alpha_{0,1}$	$\alpha_{0,1}\alpha_{0,1}$	$\alpha_{0,1}\alpha_{1,2}$	$\alpha_{0,1}\alpha_{2,3}$
$\alpha_{1,2}$	$\alpha_{1,2}\alpha_{0,1}$	$\alpha_{1,2}\alpha_{1,2}$	$\alpha_{1,2}\alpha_{2,3}$
$\alpha_{2,3}$	$\alpha_{2,3}\alpha_{0,1}$	$\alpha_{2,3}\ \alpha_{1,2}$	$\alpha_{2,3}\alpha_{2,3}$

If we now define

Z = $\{(\alpha_{0,1}), (\alpha_{1,2}), (\alpha_{2,3})\}$, then we have

	$\alpha_{0,1}$	$\alpha_{1,2}$	$\alpha_{2,3}$
$\alpha_{0,1}$	$Z\alpha_{0,1}$	$Z\alpha_{1,2}$	$Z\alpha_{2,3}$
$\alpha_{1,2}$	$Z\alpha_{0,1}$	$Z\alpha_{1,2}$	$Z\alpha_{2,3}$
$\alpha_{2,3}$	$Z\alpha_{0,1}$	$Z\alpha_{1,2}$	$Z\alpha_{2,3}$

as well as

	$\alpha_{0,1}$	$\alpha_{1,2}$	$\alpha_{2,3}$
$\alpha_{0,1}$	$\alpha_{0,1}Z$	$\alpha_{0,1}Z$	$\alpha_{0,1}Z$
$\alpha_{1,2}$	$\alpha_{1,2}Z$	$\alpha_{1,2}Z$	$\alpha_{1,2}Z$
$\alpha_{2,3}$	$\alpha_{2,3}Z$	$\alpha_{2,3}Z$	$\alpha_{2,3}Z$,

Hence, if we take the structure $Z\alpha_{i,j}$, where the $[\alpha_{i,j}]$ are left-adjoint, the result is a matrix of the triads, but if we take the structure $\alpha_{0,1}Z$, where the $[\alpha_{i,j}]$ are right-adjoint, the result is a matrix of trichotomies. However, the most astonishing result is that now dual (converse) sub-signs are no longer identical inside, but between the two matrices

$$Z\alpha_{1,2} \neq Z\alpha_{0,1} \wedge \alpha_{0,1}Z \neq \alpha_{1,2}Z, \quad \text{but} \quad Z\alpha_{1,2} = \alpha_{0,1}Z$$
$$Z\alpha_{2,3} \neq Z\alpha_{0,1} \wedge \alpha_{0,1}Z \neq \alpha_{2,3}Z, \quad \text{but} \quad Z\alpha_{2,3} = \alpha_{0,1}Z$$
$$Z\alpha_{2,3} \neq Z\alpha_{1,2} \wedge \alpha_{1,2}Z \neq \alpha_{2,3}Z \quad \text{but} \quad Z\alpha_{2,3} = \alpha_{1,2}Z.$$

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